

COMPUTATIONAL EXPLORATION OF CONFLICT DYNAMICS THROUGH LANCHESTER'S EQUATIONS WITH PYTHON

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This study investigates the computational modeling of conflict dynamics between opposing forces using Lanchester's equations, implemented via Python's numerical odeint solver (the library). By transforming classical attrition models into computational simulations, it becomes possible to explore how variations in force strength, combat efficiency, and reinforcement timing influence battle outcomes.

At the core of this work is the analysis of how two sides interact over time under changing strategic conditions. Even slight improvements in one side's efficiency-reflecting tactical upgrades, technological advancements, or improved coordination can lead to faster victories and reduced casualties. This demonstrates the critical importance of quality over quantity in strategic planning.

Reinforcement strategies are examined both continuously and with time delays. Early or strategically timed reinforcements can shift the direction of the conflict dramatically. Conversely, delaying the opponent's reinforcements-even slightly-can prevent defeat and reverse the trajectory of battle. The simulations clearly illustrate these turning points and show how troop numbers evolve over time under different assumptions.

The model further incorporates third-party influence, where external support dynamically alternates between the two sides. This reflects real-world scenarios where alliances and aid can shift mid-conflict, altering momentum and reshaping outcomes. An additional scenario demonstrates that reallocating a small fraction of one's own resources to delay the enemy's reinforcement can be a decisive move, emphasizing the value of foresight and timing over brute strength.

Through these scenarios, the results highlight that outcomes are not solely determined by initial force levels, but by the interplay of efficiency, timing, and strategy. The modeling framework provides a robust tool for strategic analysis, with potential applications beyond military theory-including business competition, resource allocation, and game strategy. It also serves as an educational resource for exploring differential systems in applied contexts.

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1. Raynovskyy I. Lanchester's equations in conflicting sides using ODEINT Python library. In. Analytical and Approximate Methods for Complex Dynamical Systems, Ch.6, Springer, 2025, pp.89-100.