

STABILIZERS OF MORSE-BOTT FUNCTIONS ON SURFACES AND THEIR HOMOTOPY TYPE

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Let M be a smooth compact surface, P be either \mathbb{R} or S^1 , and $\mathcal{D}(M)$ be a group of C^∞ -diffeomorphisms of M . For a smooth function $f \in C^\infty(M, P)$ we denote by $\mathcal{S}(f)$ the stabilizer of f , i.e., a subgroup of $\mathcal{D}(M)$ of f -preserving diffeomorphisms of M , and by $\mathcal{S}_{\text{id}}(f)$ a connected component of the identity map of the group $\mathcal{S}(f)$.

The report will be devoted to the description of the homotopy type of $\mathcal{S}_{\text{id}}(f)$ for P -valued Morse-Bott functions on surfaces. We proved that $\mathcal{S}_{\text{id}}(f)$ is contractible if f has at least one saddle point or M is non-oriented, and to S^1 otherwise. Moreover, the result holds for some larger class of smooth functions, see [1].

1. Feshchenko B., Homotopy type of stabilizers of circle-valued functions with non-isolated singularities on surfaces, arXiv:2305.08255