The continuity of Darboux injections between manifolds

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We shall discuss a problem of Willie Wong who asked on Mathoverflow if every bijective Darboux map $f: X \to Y$ between Eculidean spaces (more generally, between manifolds) is a homeomorphism. A function between topological spaces is *Darboux* if the image of any connected subset is connected. We prove that an injective Darboux map $f: X \to Y$ between connected metrizable spaces X, Y is continuous if one of the following conditions is satisfied:

(1) Y is a 1-manifold and X is compact;

(2) Y is a 2-manifold and X is a closed 2-manifold;

(3) Y is a 3-manifold and X is a rational homology 3-sphere.

More details can be found in the preprint https://arxiv.org/abs/1809.00401.