On polynomial identities in algebras generated by idempotents and its *-representations

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We concider algebras $P_{n,\overline{\lambda}}$ that are generated by indepotents p_1,\ldots,p_n connected by linear relation $\lambda_1p_1+\cdots+\lambda_np_n=e,\ \lambda_i\in\mathbb{C}\{0\}$. It is proved that $P_{n,\overline{\lambda}}$ is the algebra without polynomial identities for n>4 and for $n=4,\ \lambda_1+\lambda_2+\lambda_3+\lambda_4\neq 2$. Also it is shown that $P_{4,\overline{\lambda}}$ are F_4 -algebras if $\lambda_1+\lambda_2+\lambda_3+\lambda_4=2$. It is found some example of F_6 -algebras in set of algebras $P_{n,\lambda}/\{p_{i_l}p_{j_l}=p_{j_l}p_{i_l}=0\}_{l=1}^m$ where $i_l\neq j_l\in\{1,\ldots,n\}$.