

**Title :** The Integrals of Motion for  
the elliptic deformed  $W$ -algebra

**Subtitle :** An elliptic quantization of the KdV theory

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**Abstract :**

We construct infinitely many commutative operators associated with the elliptic deformation of the  $W$ -algebra. The quantum version of the KdV theory is the CFT (conformal field theory) governed by the  $W$ -algebra. This CFT has infinitely many commutative operators, which can be regarded as a quantization of the integrals of motion for the KdV [BLZ]. In this talk we construct elliptic deformation of this CFT. We construct infinitely many commutative operators associated with the elliptic deformation of the  $W$ -algebra  $W_{q,t}(\widehat{sl}_N)$  [KS]. In addition, we discuss the level parameter generalization of the commutative operators, which are governed by a parameter extension of the deformed  $W$ -algebra [K].

**References**

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[KS] T.Kojima and J.Shiraishi : The Integrals of Motion for the Deformed  $W$ -Algebra  $W_{q,t}(\widehat{sl}_N)$ .II.Proof of the Commutation Relations, *Commun.Math.Phys.***283**, 795-851, (2008).  
[K] T.Kojima : Wakimoto realization for the elliptic quantum group  $U_{q,p}(\widehat{sl}_N)$ , to appear in *Int.J.Mod.Phys.A*, [nlin.SI.0902.1022].