Cosmological symmetry breaking and generation of electromagnetic field

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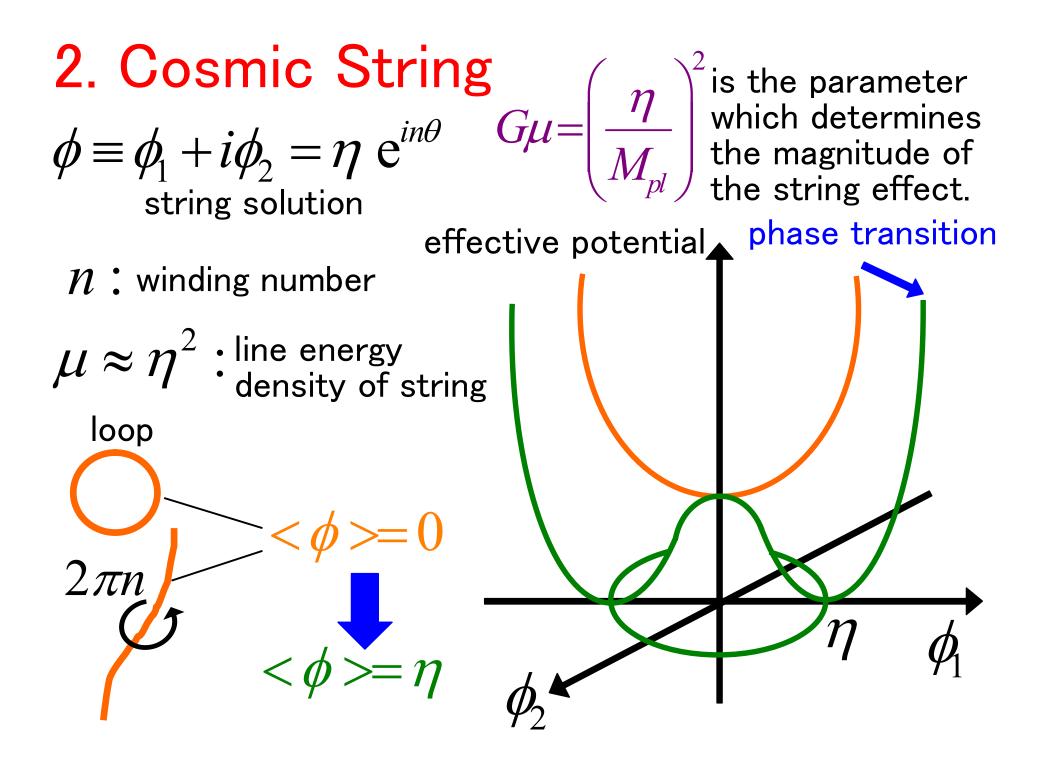
1. Introduction

Embedded defects are unstable at zero temperature.

In the early universe, the finite - temperature plasma existed.

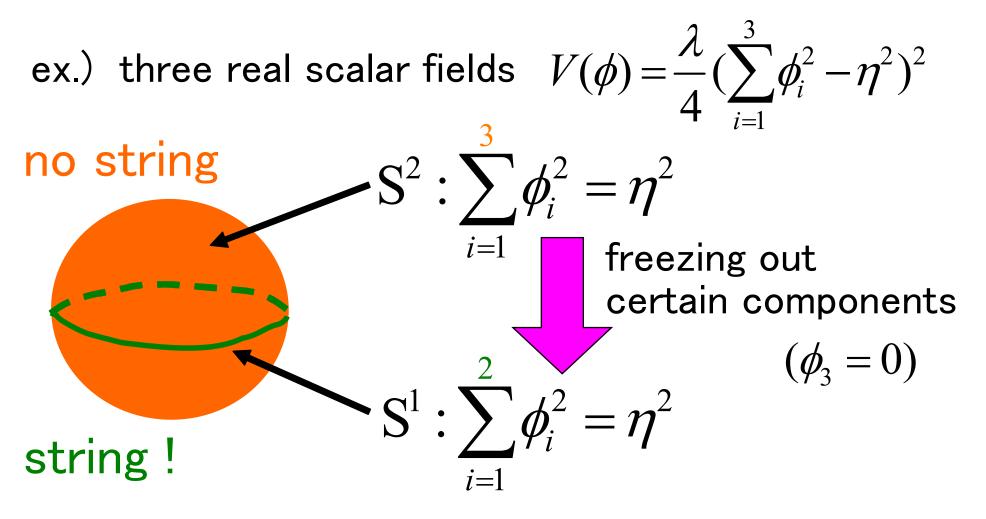
They can be stabilized because of the asymmetry between charged and neutral scalar components.

At the low temperature, the photon decoupling occurs. Defects undergo core phase transition and/or decay. primordial magnetic field ? Some kinds of effects on cosmic microwave background radiation could be observed.



3. Embedded String

Although the configuration of embedded defects satisfies equations of motion, they are topologically, and in general also dynamically unstable.



4. Pion String

one example of embedded <mark>global</mark> string

standard model of strong interaction

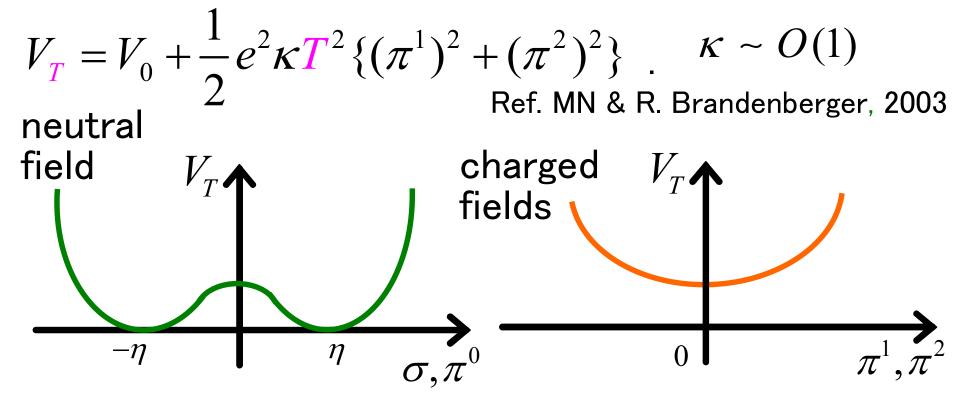
 $\begin{array}{c} & \bigoplus \\ & \mathsf{QCD} \text{ phase transition} \, (\cong 200 \text{ MeV}) \\ & \mathsf{Below the confinement scale, this model is described} \\ & \mathsf{by a sigma model involving the sigma field } \sigma \text{ and the} \\ & \mathsf{three pions } \vec{\pi} = (\pi^0, \pi^1, \pi^2) \cdot \\ & L_0 = \frac{1}{2} \partial_\mu \sigma \partial^\mu \sigma + \frac{1}{2} \partial_\mu \vec{\pi} \partial^\mu \vec{\pi} - V_0 \\ \end{array}$

cf. Although it is different from the cosmological scenario, following the Kibble–Zurek mechanism the pion strings are expected to be formed in LHC Pb – Pb collision experiments. These effects could be observable and bring distinction compared to conventional predictions.

Ref. H. Mao, Y. Li, MN, X. Zhang & T. Huang, 2005

5. Finite Temperature Effect

When the background photon plasma can be regarded as a thermal bath, the interaction between charged fields and photon could be included into the effective potential as



By analyzing the stability of the pion string solution under simple assumptions, the destabilization temperature can be calculated as $T_{_D}=2\lambda^{1/2}\kappa^{-1/2}e^{-1}\eta$.

6. Core Phase Transition

The results of numerical simulations show that even below T_D , the string does not decay. Actually the Higgs field has a finite expectation value at the string core and the neutral field configuration is not destroyed, which means that a core phase transition occurs. • • Since the winding number is

a kind of topological charge, finite temperature it must be conserved. effect domination 0 sufficiently low temperature T_D neutral (π^0) field charged $+(\pi^{2})^{2}$ field

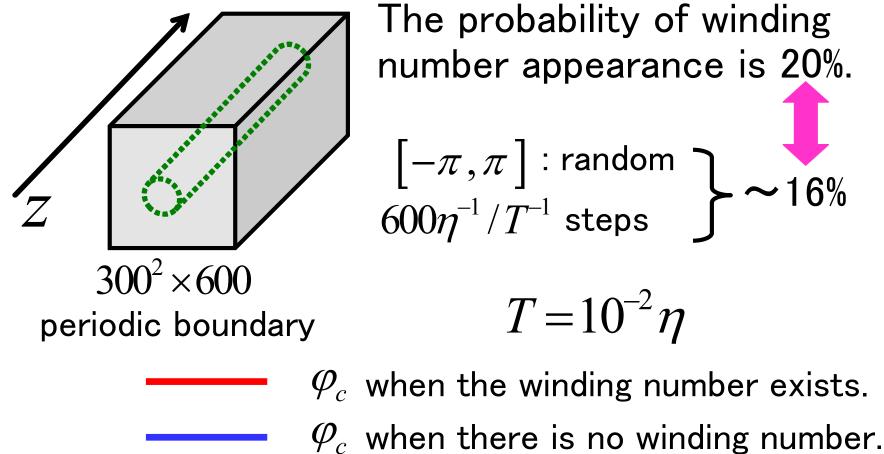
7. Superconductivity

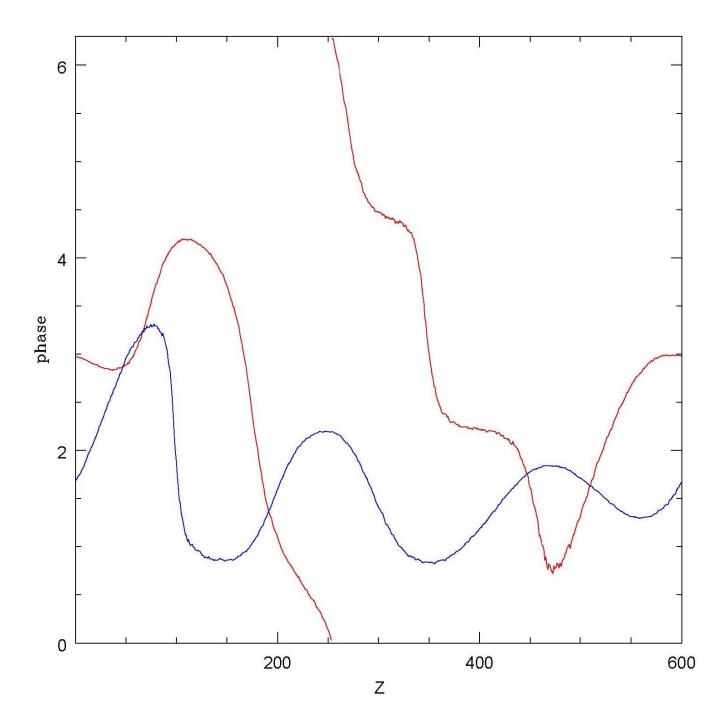
After the core phase transition, charged fields have finite expectation value and the phase has a spatial gradient along the string so that the electric current will be generated.

$$\sqrt{\left(\pi^{1}\right)^{2} + \left(\pi^{2}\right)^{2}} = \phi_{c}\left(x, y\right)e^{i\varphi_{c}(z,t)}$$

current amplitude ~ $e\frac{d\varphi_{c}}{dz}$
infinite strings
infinite strings
Infinitely long strings and/or loops of large curvature radius
could show a filament-like spatial distribution feature.
astrophysical counterparts: gravitational lensing?

8. 3-dimensiocal simulation A initially translation symmetric string evolution is solved in a 3-dimensional box and the distribution of φ_c shows the winding number appears in some cases.





9. Interaction of Scalar Field with Electromagnetic Field

In general, the following type of interaction between the electromagnetic filed and a certain kind of field would appear in the Lagrangian when the anomaly or the Chern–Simons term is taken into account.

$$L = L_{EM} + L_{int}$$
; $L_{int} = -\frac{1}{2}O_{\mu}A_{\nu}\varepsilon^{\mu\nu\alpha\beta}F_{\alpha\beta}$

Then the equations of motion for electromagnetic field should be modified so that the generation of magnetic field and/or the polarization of background radiation would occur because of the field, O_{μ} .

$$\partial_{\mu}F^{\mu\nu} = 4\pi J^{\nu} + O_{\mu}\varepsilon^{\mu\nu\alpha\beta}F_{\alpha\beta}$$

ex.) axion, type IIB string model...

10. Magnetic Filed Generation from
Pion StringsR. Brandenberger & X. Zhang, 1999

In case of the pion string, there exists an interaction between the pion field π^0 and the electromagnetic field.

$$L_{\rm int} = -\frac{N_c \alpha}{24\pi} \frac{\pi^0}{f_{\pi}} \varepsilon^{\mu\nu\alpha\beta} F_{\mu\nu} F_{\alpha\beta} \qquad \begin{array}{l} N_c = 3\\ \alpha : \text{ fine structure constant} \end{array}$$

Zero mode current appears within the string core and the azimuthal magnetic field is produced.

$$B_{\theta} = -N_c \frac{eT_c}{2\pi} \left(\frac{r}{\delta_s}\right)^{\alpha/\pi} \frac{1}{r} \qquad \delta_s \approx f_{\pi}^{-1} \cdot \frac{\text{string}}{\text{core radius}}$$

At the recombination, $B(T_{\text{rec}}) \approx 10^{-23} \left(\frac{r}{\delta_s}\right)^{\alpha/\pi} \frac{1 \text{kpc}}{r} \text{ G}$.
$$T = T_c \qquad \text{present}$$

11. Helicity of Magnetic Field

If the twist and tangle of strings are biased when the CP violation exists, then the helicity of magnetic field is also biased so that its conservation leads to the generation of larger magnetic field amplitude.

helicity density :
$$\begin{split} \mathbf{H} &= \frac{1}{V} \int_{V} d^{3} x \mathbf{A} \cdot \mathbf{B} \\ \text{After the phase} \\ \text{transition,} \\ \mathbf{H} \approx \varepsilon_{CP} 4 N_{c}^{-2} \left(\frac{\xi_{s}}{T^{-1}}\right)^{-2+\alpha/\pi} \left(\frac{f_{\pi}}{T}\right)^{1+\alpha/\pi} T^{3} \end{split}$$

 \mathcal{E}_{CP} : CP violation strength ξ_s : correlation length of strings It can be shown that the helicity is not erased and according to the most optimistic estimation, on the scale of 1pc, at the recombination, $B \approx 10^{-9}$ G. 12. Modified Maxwell Equation Next it is considered how the same interaction affects the light propagation. $L_{\rm int} = -\frac{N_c \alpha}{24\pi} \frac{\pi^0}{f_{\pi}} \varepsilon^{\mu\nu\alpha\beta} F_{\mu\nu} F_{\alpha\beta}$

If the time evolution of string distribution can be neglected, then the equations without the current under the string background will be written as

$$\begin{cases} \nabla \mathbf{E} = -\mathbf{\Phi} \cdot \mathbf{B} \\ -\frac{\partial \mathbf{E}}{\partial t} + \nabla \times \mathbf{B} = \mathbf{\Phi} \times \mathbf{E} \end{cases} \quad \mathbf{\Phi} \equiv \frac{N_c \alpha}{3\pi} \nabla \frac{\pi^0}{f_{\pi}} \quad \mathbf{\Phi} \end{cases}$$

φ

and the dispersion relation becomes $\sqrt{-1/2}$

$$k^{2} = \omega^{2} \pm \omega \Phi \cos \varphi \left(1 - \frac{\Phi^{2} \sin^{2} \varphi}{\omega^{2} - k^{2}} \right)^{-1}$$

13. Rotation of Polarization Axis

Under the approximation that $\Phi = \omega \pm \frac{\Phi}{2} \cos \varphi$. $k \cong \omega \pm \frac{\Phi}{2} \cos \varphi$.

Thus the rotation angle difference of polarization axis between left-handed polarization and right-handed one, $\Delta \psi$, can be estimated as follows dependent on the direction of the string axis to the line of sight.

When the light travels perpendicular to the string, $\Delta \psi \approx 10^{-3}$,

which is the maximum value. Note that the sign depends on which side the light passes. When the light travels in parallel with the string $\Delta \psi \approx 0$.

➢In any cases, the distance between the string and the light path is not so significant.

14. Summary

It is considered that the magnetic field generation by pion strings produced at the QCD phase transition and the interaction of this magnetic field with the cosmic background radiation.

- •Magnetic field strength generated by pion strings depends on the distance to the string axis and it is sufficiently high when the effective α is large.
- •In the case that the bulk helicity exists, although the amplitude of magnetic field would be enhanced, the correlation scale should be smaller.
- •It is shown that the rotation of light polarization axis is caused by the string field and the spatial distribution of rotation angle directly traces the arrangement of the strings in our universe.